

# IMPLEMENTATION OF CLOCK GATING LOGIC BY MATCHING FACTORED FORMS

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**Abstract** — Clock gating is one among the most widespread circuit technique to scale back power consumption. Clock gating is sometimes done at the register transfer level (RTL). Automatic synthesis of clock gating in gate level has been less explored, however it's certainly additional convenient to designers. Clock gating consists of 2 steps: extraction of gating conditions by merging gating conditions of individual flip-flops, implementation of the gating conditions with minimum quantity of further gates. In this paper, We show a way to do factored form matching, within which gating operates in factored kinds are matched, as way as possible, with factored kinds of the mathematician functions of existing combinable nodes within the circuit; further gates are then introduced, however just for the portion of gating functions that don't seem to be matched. sturdy matching identifies matches that are explicitly given within the factored forms, and weak matching seeks matches that are implicit in the logic and so are tougher to get.

**Keywords:** Clock gating, gating function, factored form.

## 1. INTRODUCTION

Clock gating is a well understood power optimization technique employed in both ASIC and FPGA designs to eliminate unnecessary switching activity. This method usually requires the designers to add a small amount of logic to their RTL code to disable or deselect unnecessarily active sequential elements, e.g. registers.

The condition in which clock is gated, called a gating function, is typically specified by designers during RTL design stage; the logic for this condition is added by the designers. A prime example is a load-enable register, illustrated in Figure 1(a). When EN is 0, the register keeps the current value of Q; otherwise D is loaded at the next clock edge. A gating function generates EN in this case.

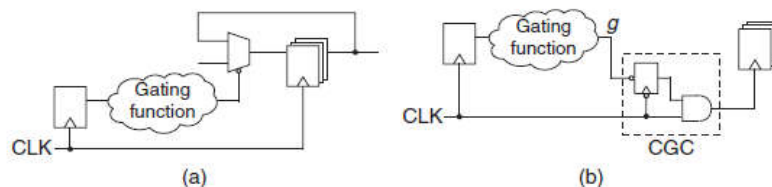


Fig. 1. Load-enable registers

(a) before and (b) after clock gating

Clock gating can be applied by using a circuit shown in Figure 1(b), which is functionally equivalent to Figure 1(a). The multiplexer is removed and the clock signal itself is gated with the EN signal. A circuitry within the dotted box is called a clock gating cell (CGC); a latch is needed to remove any glitches in EN. Relative to the case in Figure 1, clock gating strategies can be considerably more sophisticated in real circuits and generally involve analysis of when registers may be kept idle and subsequent synthesis of clock gating (EN) signals which is determined by the designers.

RTL clock gating has two significant limitations: 1) the designer has to provide a gating function and 2) registers whose gating functions are not specified are left ungated. One way to resolve these problems is to take each ungated register, connect its input and output to an exclusive-NOR gate, and use the output of that gate as a gating function of register. However, this technique can only be applied when the register input arrives sufficiently early so that a delay through the exclusive-NOR gate and the CGC can be tolerated.

In this paper, we propose a new technique to simplify gating functions. The idea is to use the existing logic as far as possible while the gating functions are synthesized. This is achieved by matching factored forms of the gating functions with those of existing logic nodes, thus we call this technique as factored form matching. We will present two matching methods: 1) strong matching (SM), which looks for matches that are explicitly apparent in an expression of the circuit logic and 2) weak matching (WM), which seeks matches that are logically present but cannot be found by inspection. Experiments on test circuits show reductions in the area of gating functions between 11% and 39%, with an average of 24%. We contrast these results with those from Boolean division in which, on average, 8% reduction is observed. The rest of this paper is organized as follows. Factored form matching is introduced in Section 2, and the matching algorithm is presented and analyzed. In Section 3, we present our experimental results, and, finally, a conclusion is summarized in Section 4.

## 2. FACTORED FORM MATCHING

If we have a set of gating functions  $\{F_1, F_2, \dots\}$ , such that each  $F_i$  enables ( $F_i = 0$ ) and disables ( $F_i = 1$ ) the clock to a set of flip-flops. Each gating function can be represented in a factored form, or equivalently as a factoring tree, which we will assume to be binary. Our task is to find some existing logic of a combinational circuit, which, together with a few extra gates, implements a gating function. Simultaneously, we have to maximize the proportion of the gating function that is provided by existing logic, so as to minimize the number of extra gates. Because the existing logic can also be represented as a factoring tree, the problem can be recast as that of finding the parts of a factoring tree of a gating function that can be replaced by factoring trees taken from the existing logic; we call this process as factored form matching, which consists of SM and WM.

An overview of factored form matching is shown in Fig. 2, in which it is performed for each individual gating function  $F_i$  or  $F$  separately, so as to simplify the notation. A factoring tree of  $F$ , denoted by  $TF$ , is first obtained (L1) by factoring  $F$ , which is performed by recursive algebraic division using a kernel of  $F$  as a divisor.<sup>1</sup> Matching is then performed in two steps: 1) SM (L3–L9) and 2) WM (L10–L15).

```

Algorithm Factored_Form_Matching ( $F$ )
L1    $T_F \leftarrow \text{Factoring}(F)$ 
L2    $L_{sm} \leftarrow \emptyset, L_{wm} \leftarrow \emptyset$ 
L3   foreach internal node  $n$  do
L4     if  $n$  contains literals not in  $F$  then skip  $n$ 
L5      $T_n \leftarrow \text{Factoring}(n)$ 
L6      $\mathcal{M}_n \leftarrow \text{Strong\_Match}(T_F, T_n)$ 
L7     if  $\mathcal{M}_n \neq \emptyset$  then
L8       if  $\text{Containment}(L_{sm}, \mathcal{M}_n) \neq \text{yes}$  then
L9          $L_{sm} \leftarrow L_{sm} + (n, \mathcal{M}_n)$ 
L10    foreach unskipped internal node  $n$  do
L11       $\mathcal{M}_n \leftarrow \text{Weak\_Match}(T_F, T_n)$ 
L12      if  $\mathcal{M}_n \neq \emptyset$  then
L13        if  $\text{Containment}(L_{sm}, \mathcal{M}_n) = \text{yes}$  then skip  $n$ 
L14        else if  $\text{Containment}(L_{wm}, \mathcal{M}_n) = \text{yes}$  then skip  $n$ 
L15        else  $L_{wm} \leftarrow L_{wm} + (n, \mathcal{M}_n)$ 

Function Containment( $L, \mathcal{M}$ )
L16  foreach  $(n, \mathcal{M}_n) \in L$  do
L17    foreach pair  $(g, g')$ , where  $g \in \mathcal{M}_n$  and  $g' \in \mathcal{M}$  do
L18      if  $g \subseteq g'$  then  $\mathcal{M}_n \leftarrow \mathcal{M}_n - g$ 
L19      else if  $g' \subset g$  then  $\mathcal{M} \leftarrow \mathcal{M} - g'$ 
L20    if  $\mathcal{M}_n = \emptyset$  then  $L \leftarrow L - (n, \mathcal{M}_n)$ 
L21  if  $\mathcal{M} = \emptyset$  then return yes

```

Fig. 2. An algorithm for factored form matching:

Where  $T$  is the factoring tree,  $\mathcal{M}_n$  is the set of subtrees (in SM) or sets of vertices (in WM) of  $TF$  that are to be matched with  $T_n$ , and  $L$  is the list of the resulting pairs  $(n, \mathcal{M}_n)$ .

### A. Strong Matching

Consider the factoring tree of a gating function  $F$  shown in Fig. 3(a), and the factoring trees of three of the existing internal nodes shown in (b)–(d). The subtree of  $F$  marked  $N_1$  and the tree  $n_1$  are structured in different ways, but they actually represent the same Boolean expression  $abc+acd+bd$ ; we say that  $N_1$  and  $n_1$  are equivalent.  $N_2$  and  $n_2$  are also equivalent; in fact, these trees have the same structure, except for the ordering of children; we say that such trees are syntactically equivalent.

Finally,  $N_3$  and  $n_3$  are syntactically equivalent, and children are ordered in the same way; rather obviously, we call these identical factored forms. Any of these three types of equivalence are said to provide a strong match in this paper.

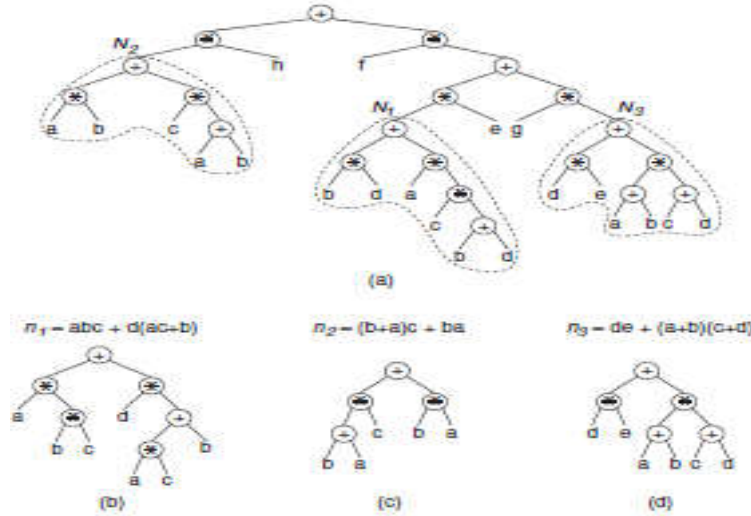


Fig. 3. Factoring trees of (a) a gating function  $F$ : of internal nodes (b)  $n_1$ , which is equivalent to subtree  $N_1$ , (c)  $n_2$ , which is syntactically equivalent to subtree  $N_2$ , and (d)  $n_3$ , which is identical to subtree  $N_3$ .

Finding the most general strong match involves the detection of equivalent factored forms. This, however, is a problem of combinational equivalence checking, which is proven to be co-NP-complete.<sup>2</sup> Thus, we focus on finding syntactically equivalent and identical factored forms in this paper.

**I) Detection of Syntactically Equivalent and Identical Factored Forms**

Pseudocode for the algorithm that we use to detect syntactically equivalent factored forms is shown in Fig. 4.  $T$  is a large factoring tree (similar to  $F$  in Fig. 3), which may contain one or more subtrees that are syntactically equivalent to a smaller tree  $t$  (such as  $n_1$  in Fig. 3). For each vertex  $v$  in  $T$ , we check whether the size of subtree rooted at  $v$ , denoted by  $T_v$ , is the same as that of  $t$  (L4); note that, we only consider  $v$  that is the same as the root of  $t$  (L2) by the definition of syntactical equivalence. Then, we label both  $T_v$  and  $t$ , level by level, starting at the deepest level.

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Algorithm Syntactically_Equivalent ( $T, t$ )
L1    $\mathcal{M} \leftarrow \emptyset$ 
L2   foreach vertex  $v \in T$ , where  $v = \text{root of } t$  do
L3      $T_v \leftarrow \text{subtree rooted at } v$ 
L4     if  $|T_v| = |t|$  then
L5       foreach level  $i$  of  $t$  and  $T_v$  from deepest do
L6          $V_v \leftarrow \text{vertices at level } i \text{ of } T_v$ 
L7          $V_t \leftarrow \text{vertices at level } i \text{ of } t$ 
L8         if Labeling ( $V_v, V_t$ ) = fail then skip  $v$ 
L9          $\mathcal{M} \leftarrow \mathcal{M} + T_v$ 
L10  Return  $\mathcal{M}$ 
    
```

Fig4. Algorithm to detect syntactically equivalent factored forms.

**II) SM Algorithm**

The procedure *Strong\_Match* called by the algorithm in Fig. 2 itself calls either *Syntactically Equivalent* or *Identical*, depending on how the factoring trees of  $F$  and the existing internal nodes  $n_i$  are obtained. We might apply quick factoring to the  $n_i$  terms to reduce runtime, and good factoring to  $F$  to obtain a smaller tree.<sup>3</sup> Because different factoring methods may use different divisors, they can yield syntactically equivalent as well as identical factored forms. On the other hand, if quick factoring is applied to both  $F$  and the  $n_i$  terms, we only need to look for identical factored forms, which takes less time. It can readily be shown that the complexity of *Syntactically\_Equivalent* is  $O(V \log V)$  and that of *Identical* is  $O(V)$ , where  $V$  is the number of vertices.

**B. Weak Matching**

In searching for a strong match between a subtree of a gating function and the factoring tree corresponding to an existing logic node, we only look for syntactically equivalent and identical factored forms, and so the two trees must have the same structure. This is a rigid requirement, especially for large trees. Consider Fig.5, in which no subtree of  $F$  strongly matches  $n$ . The vertices of  $F$  within the dotted circles collectively, however, constitute the same expression as  $n$ , because

$$F = aeg(d + f(b + c)) + abh + defg$$

$$= n(aeg) + abh + defg.$$

All the nodes n that are not skipped are checked for weak match (L10 of Fig. 2).

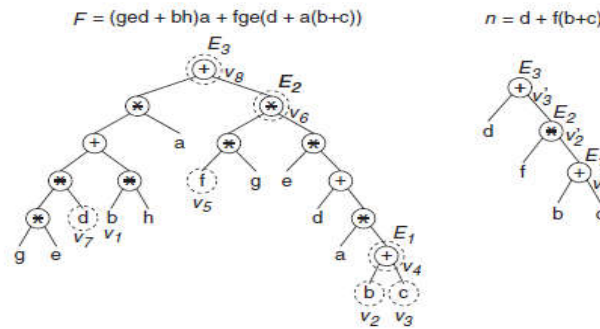


Fig5. Weak match of a gating function F with an internal node n.

**IJWM Algorithm:** WM algorithm (denoted by Weak\_Match) pseudocode is shown in Fig6. T is a large tree (like F in Fig.5), which may contain one or more sets of vertices that are weakly matched to a smaller tree t (similar to n in Fig. 5). Initially, for each vertex v in T and t, we assign its subexpression Ev and factor F(v) to v and 1, respectively (L2), subexpression of each leaf becomes itself (such as Ev5 = f) and factors for all vertices are initialized to one.

Now, we traverse the tree t in postorder. For each vertex v visited during the traverse, the expression using subexpressions of its children and operation of itself is assigned to Ev\_ (like Ev\_2 = E2 = fE1); note that, we only consider v\_ that is not a leaf (L3–L6). Tv\_ is the set of three tuples (vl, vr, and vA), all vertices of which are in T; in each tuple, vA is the LCA of vl and vr and is equal to v\_ and vl and vr have the same subexpression as left and right child of v\_ , respectively (L23–L26).

```

Algorithm Weak_Match (T, t)
L1  M ← ∅, Φ(t) ← Postorder(t)
L2  foreach vertex v ∈ T ∪ t do Ev ← v, F(v) ← 1
L3  foreach vertex v' ∈ Φ(t), where v' is not a leaf do
L4    {vl, vr} ← children of v'
L5    if v' = × then Ev' ← Evl × Evr
L6    else Ev' ← Evl + Evr
L7    Mnew ← ∅, M' ← ∅, Tv' ← Candidate(T, v', vl, vr)
L8    foreach tuple (vl, vr, vA) ∈ Tv' do
L9      F(vl) ← Factor(vl, vA) × F(vl)
L10     F(vr) ← Factor(vr, vA) × F(vr)
L11     if v' = × or (v' = + and F(vl) = F(vr)) then
L12       Ev' ← Ev', M' ← M' + {vl, vr}
L13       if v' = × then F(vA) ← F(vl) × F(vr)
L14       else F(vA) ← F(vl)
L15     if M' = ∅ then Return ∅
L16     foreach pair (V, V'), where V ∈ M and V' ∈ M' do
L17       foreach v ∈ V' do
L18         if v is a leaf and v ∈ V then skip (V, V')
L19         if v is not a leaf and v ∉ V then skip (V, V')
L20         V' ← V' + LCA(V'), Mnew ← Mnew + (V ∪ V')
L21     M ← Mnew
L22  Return M

Function Candidate (T, v', vl, vr)
L23  T' ← ∅
L24  foreach pair (vl, vr) ∈ T, where Evl = Evl and Evr = Evr do
L25    vA ← LCA(vl, vr), if vA = v' then T' ← T' + {vl, vr, vA}
L26  Return T'

Function Factor(vl, vA)
L27  if vl = vA then Return 1
L28  if parent of vl = × then
L29    Return Factor(parent of vl, vA) × expression of sibling of vl
L30  else Return Factor(parent of vl, vA)
    
```

Fig6. Algorithm to detect weak matches.

For each three-tuple (vl, vr, and vA) in Tv', we find two factors F(vl) and F(vr) by ANDing their initial factors and the expression obtained from Factor (L27–L30). If the check passes, Ev A is assigned to Ev' and F(vA) is initialized either to F(vl) × F(vr) when vA is a × operation or to F(vl) when vA is a + operation, and a set of vl and vr is added to M', which is a set of sets of vertices that are matched to the children of v' (L8–L14). If M' is empty, because no vertex in T matched to v' exists, we return empty set (L15).

Otherwise, we pick a pair  $(V, V')$ , which, respectively, are extracted from  $M$  and  $M'$ , one by one;  $M$  is a set of sets of vertices in  $T$  matched to the vertices that are already traversed in  $t$ . We then, for each vertex  $v$  in  $V'$ , check if  $v$  is a leaf and not contained in  $V$  or if  $v$  is not a leaf and contained in  $V$ ; if all  $v$  satisfy the check condition, we unify  $V, V'$ , and LCA of  $V'$  power 4 and add it to  $M$  new by which  $M$  will be replaced (L16–L21).

**C. Factored Form Matching**

$L$  in Fig. 2 is the list of pairs  $(n, Mn)$ ; in each pair  $n$  is an internal node of a combinational circuit and  $Mn$  is a set of subtrees (or sets of vertices) of  $TF$  that matches with  $Tn$ , which is a factoring tree of  $n$  (L5). Two lists  $Lsm$  and  $Lwm$  are initialized and then updated to track strong and WM, respectively (L2).

We restrict our Boolean manipulation to algebraic to limit computation time; therefore, if a node  $n$  contains literals that are not in  $F$ , then  $n$  is dropped from further matching attempts (L4).

I) Containment in SM: `Strong_Match` returns a set of subtrees (L6). We can use the function `Containment` to check whether some of these subtrees are redundant because they are contained in subtrees that are already determined to be strong matches.

Example : Consider Fig. 7, in which the tree  $n_1$  is to be matched with subtrees  $N_1$  and  $N_2$ . We set  $Mn_1 = \{N_1, N_2\}$  and  $Lsm = \{(n_1, Mn_1)\}$  (L9). We continue to determine  $Mn_2 = \{N_3\}$ . Then, we perform the containment check because  $N_2 \subset N_3$ ,  $N_2$  can be discarded and we update  $Mn_1 = \{N_1\}$  (L18) and  $Lsm = \{(n_1, Mn_1), (n_2, Mn_2)\}$ . Similarly,  $Mn_3 = \{N_4\}$ , and  $N_1 \subset N_4$ . Discarding  $N_1$  makes  $Mn_1$  empty. Thus,  $(n_1, Mn_1)$  can also be discarded from  $Lsm$  (L20), and finally  $Lsm = \{(n_2, Mn_2), (n_3, Mn_3)\} = \{(n_2, \{N_3\}), (n_3, \{N_4\})\}$ .

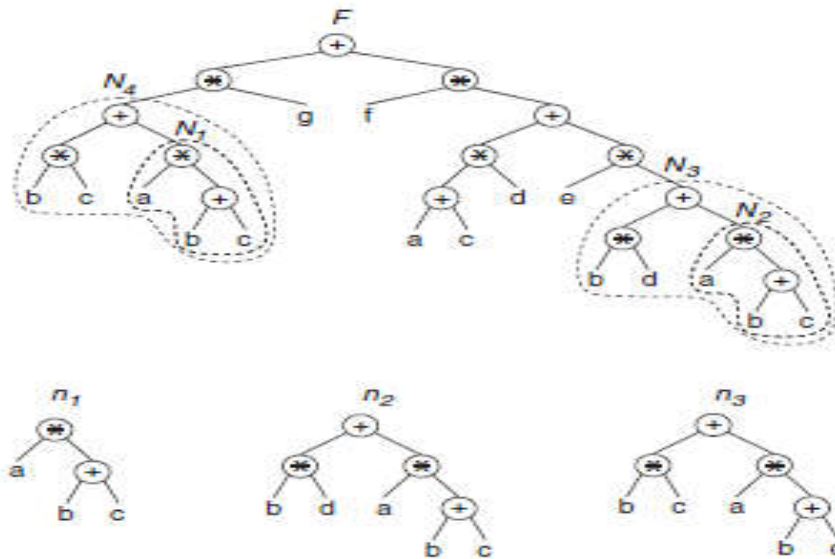


Fig7. Checking for subtree containment in SM.

We might think that the subtrees that are determined as strong matches might have a partial mutual intersection without one being wholly contained in the other; but this never happens, as we show by proving the following proposition.

Proposition 1: Let,  $n_i$  and  $n_j$  be strong matches with subtrees  $N_i$  and  $N_j$  of  $F$ , respectively. If  $N_i \cap N_j = \emptyset$ , then either  $N_i \subseteq N_j$  or  $N_j \subseteq N_i$ .

II) Containment in WM: Now, we turn our attention to the possibility of nested matches: each weak match is checked to see whether it is contained in or contains other strong or weak matches (L12–L15).

Example: Consider Fig8:  $n_1$  and  $n_2$  are strong matches with subtrees  $N_1$  and  $N_2$ , respectively. The set of vertices of  $F$  that weakly matches with  $n_3$  includes  $N_1$ ; thus  $n_1$  is dropped from the list of strong matches. The vertices that weakly match with  $n_4$  make  $n_3$  redundant. The three vertices of  $F$  that weakly match with  $n_5$  constitute a subset of  $N_2$ ; thus  $n_5$  is also redundant. Matches  $n_2$  and  $n_4$  remain after the containment check.

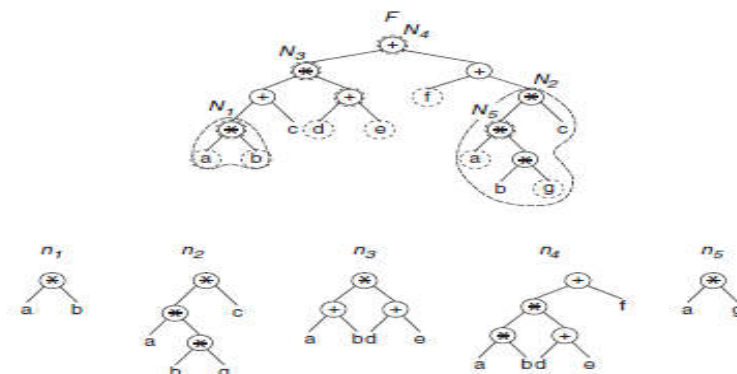


Fig. 8. Finding nested matches:  $n_1$  and  $n_2$  are strong matches and the remainders are weak matches.

### 3.EXPERIMENTAL RESULTS

To assess factored form matching (denoted by Matching in Table 1), we implemented two additional methods of simplification: using Boolean division, in which approximation, in which product terms (in sum-of-products form of a gating function) whose probability is smaller than 0.001 are declared as don't-care set, a new gating function is submitted to two level minimization followed by implementation in multi-level logic. The number of gates to implement gating functions without any simplification, given in the second column of Table 1, serves as a reference to compute the difference of the number of gates (denoted as Diff) of each simplification method.

Division achieves about 10% reduction in the number of gates, but there is wide variation (from 0% to 34%). This is expected since the existence of larger divisor relies on a chance, in particular when algebraic division is applied. Approximation achieves more reduction, but this comes at the cost of reduced gating probability. Average gating probability of gated flip-flops is 0.67 in 'No simplification', while that of Approximation is 0.62; note that Division and Matching do not sacrifice gating probability.

Matching achieves substantial reduction in gate count compared to both division and approximation. The matching takes about 10% more runtime than division method in our current implementation, ranging from 1 to 340 seconds (the last column of Table 1). The majority of runtime is due to the detection of weak matches as can be expected from its complexity. Weak matches account for only 10% of total number of matches; its contribution in gate count reduction (the second last column of Table 1) however is 25%, which demonstrates its importance in the factored form matching.

Table 1: Number of extra gates to implement gating functions. 'No simplification' serves as a reference to compute difference

Circuit	No simplification	Division		Approximation		Matching		
	# Extra gates	# Extra gates	Diff. (%)	# Extra gates	Diff. (%)	# Extra gates	Diff. (%)	Run-time (s)
s1422	78	52	-33.2	54	-30.8	32	-59.0	4.7
s3378	205	282	-7.5	279	-8.5	264	-13.4	12.7
s9234	148	136	-8.1	127	-14.2	121	-18.2	11.2
s12207	284	264	-7.0	260	-8.5	232	-18.3	10.8
s15850	431	414	-3.9	366	-15.1	367	-14.8	63.25
s35932	1401	1401	-	1234	-4.8	1255	-10.4	233.0
s38584	1317	1202	-1.1	1277	-2.0	1215	-7.7	268.7
b04	65	61	-7.6	55	-16.7	47	-28.8	26.8
b07	30	30	-	30	-	21	-30.0	19.5
b12	200	280	-6.7	271	-9.7	236	-21.3	44.3
b17	280	272	-5.9	279	-3.5	246	-14.9	339.9
ac97	67	44	-34.3	37	-44.8	24	-64.2	2.1
i2c	184	168	-8.7	166	-9.8	153	-16.8	14.7
flr	223	211	-5.4	201	-9.9	189	-15.2	12.8
mem_ctrl	611	600	-1.8	512	-16.2	486	-20.5	267.4
pe2	57	41	-28.1	41	-28.1	37	-35.1	22.5
sas	119	101	-15.1	97	-18.5	91	-23.5	5.5
systemcs	287	253	-11.8	233	-18.8	225	-21.6	57.7
usb_top	158	134	-15.2	96	-40.5	81	-48.7	31.8
wh_dma	606	538	-11.2	575	-5.1	516	-14.9	300.0
Average			-10.6		-15.6		-24.9	

### 6.1. PROPOSED METHOD RESULTS

In this chapter all the simulation results which are done using Xilinx ise 9.1 are shown in below results.

#### A. SIMULATION RESULTS

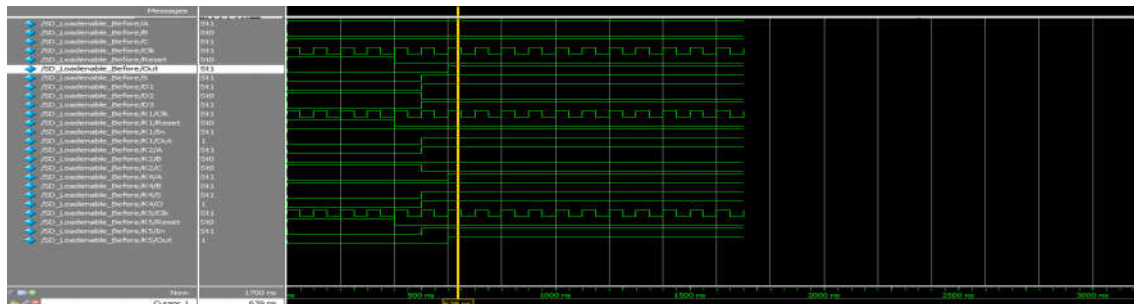


Fig 1: BEFORE CLOCK GATING

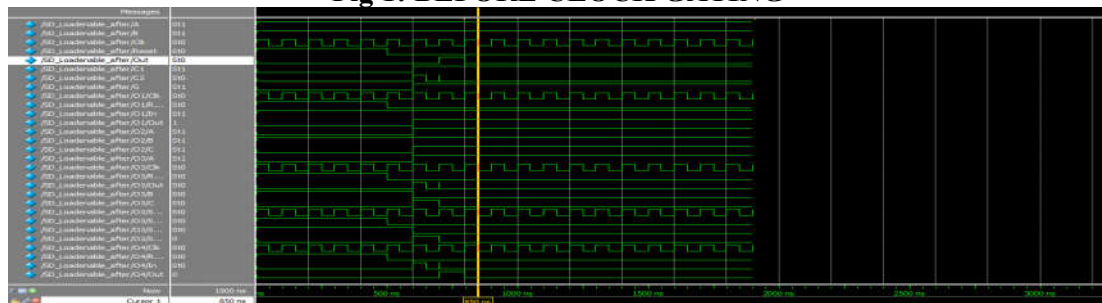


Fig 2: AFTER CLOCK GATING

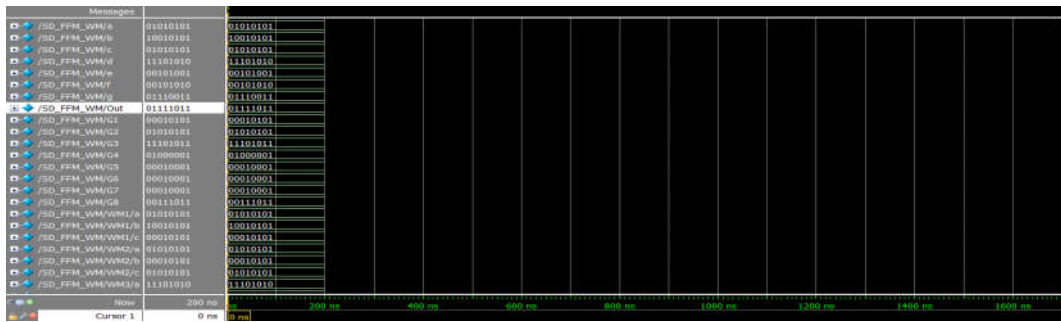


Fig 3: MATCHED FACTORED FORMS: WEAK MATCHING

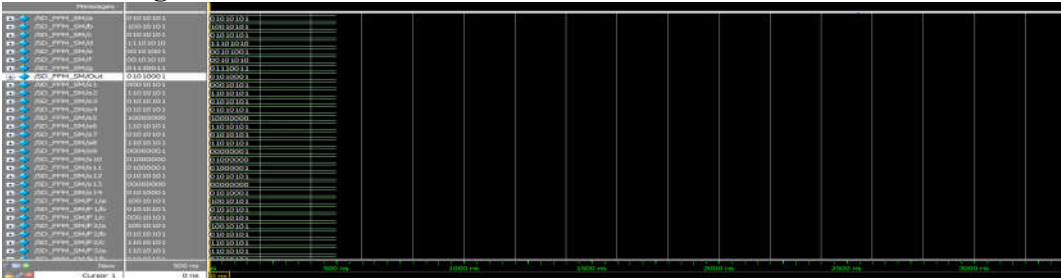


Fig 4: MATCHED FACTORED FORMS: STRONG MATCHING

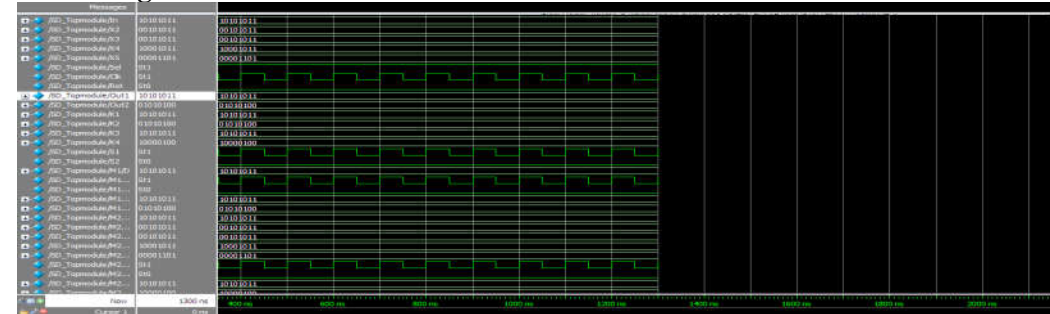
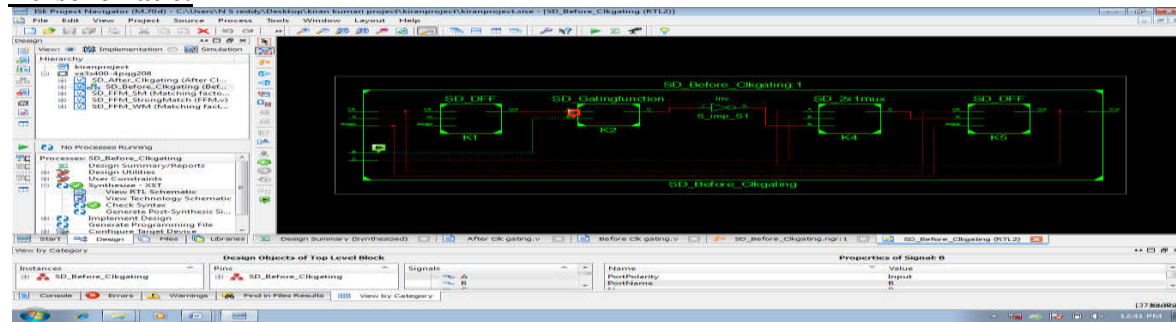


Fig 5: C17 CIRCUIT IMPLEMENTATION

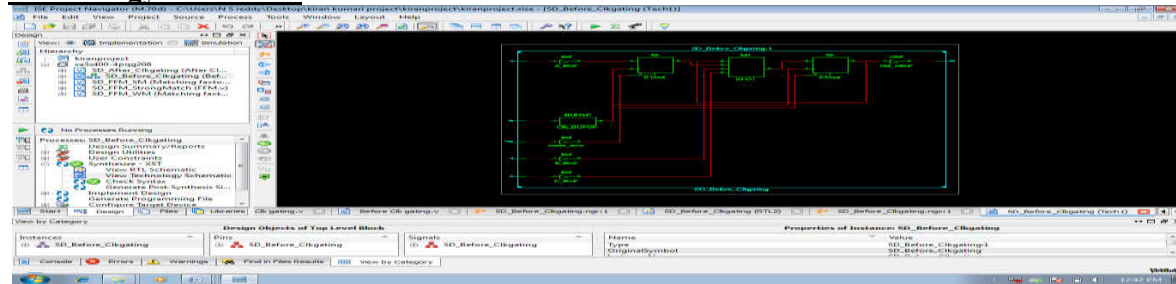
**B. SCHEMATIC DESIGNS:**

**1. Before clock gating:**

Rtl schematic:

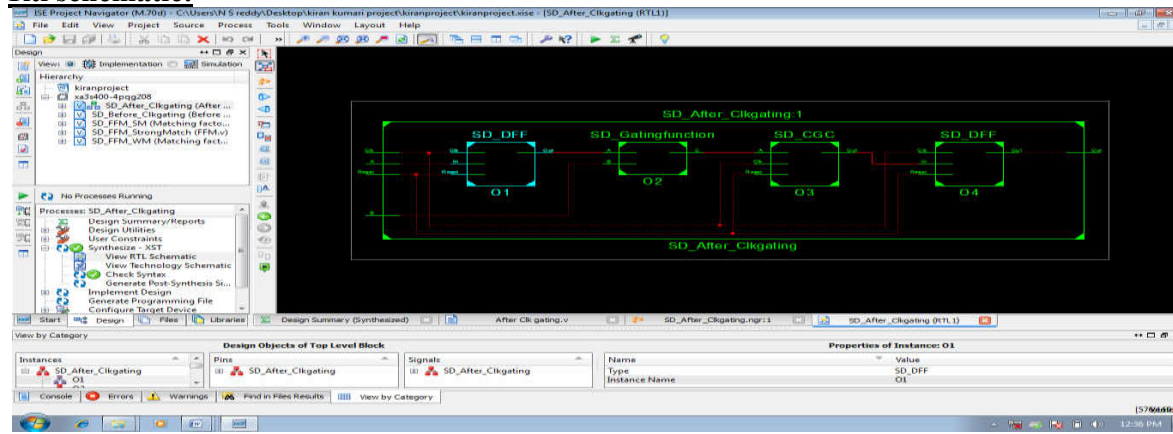


Technology schematic:

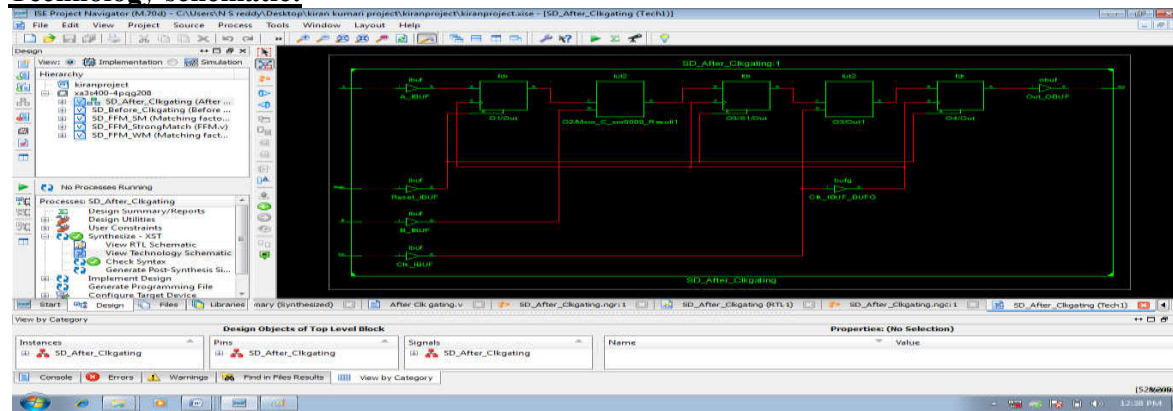


## 2. After clock gating:

### Rtl schematic:

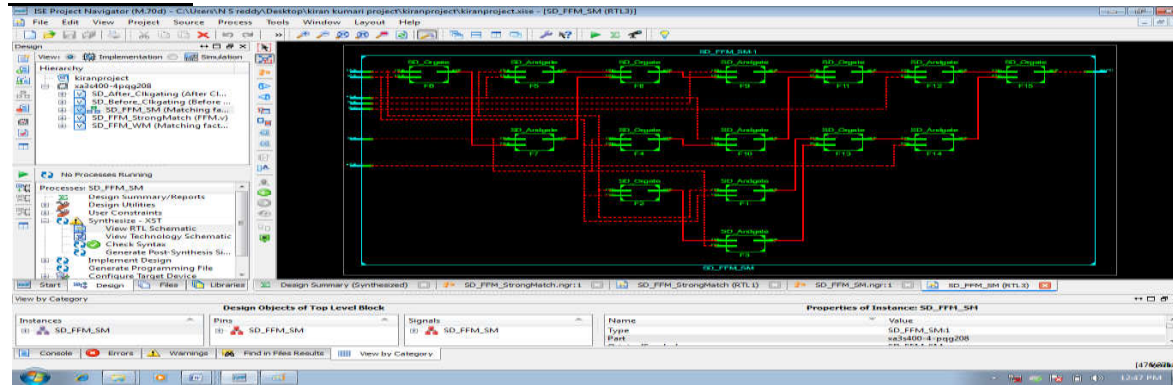


### Technology schematic:

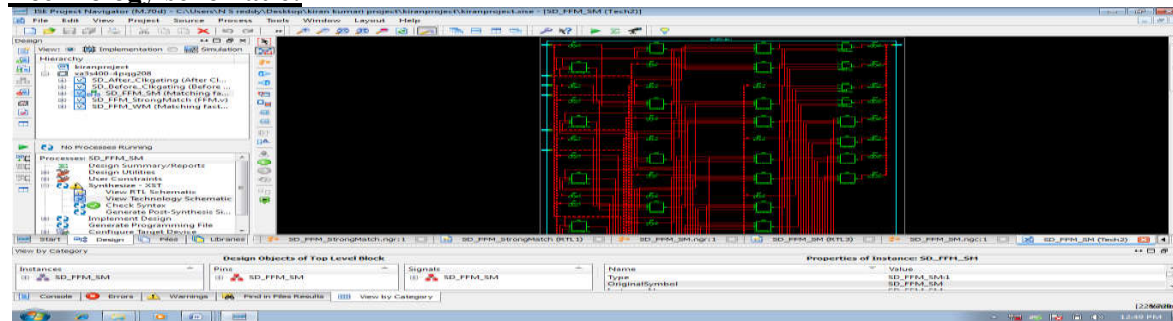


## 3. Strong matching:

### Rtl schematic:



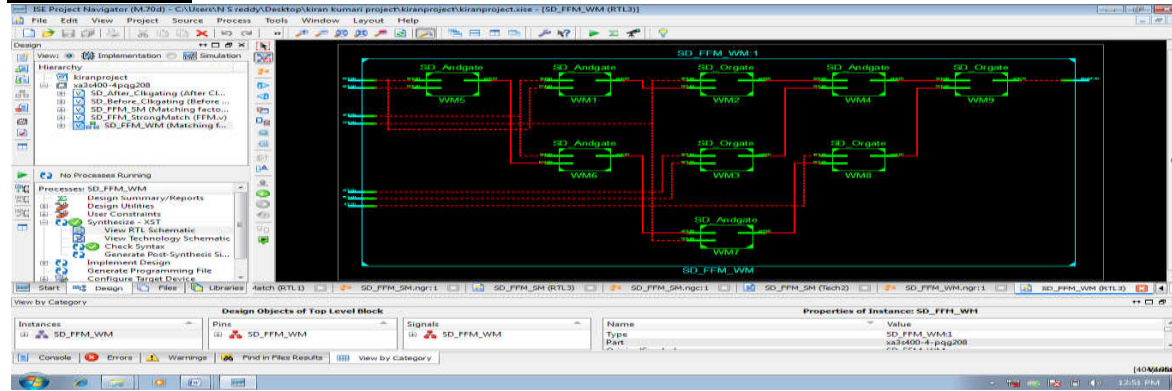
### Technology schematic:



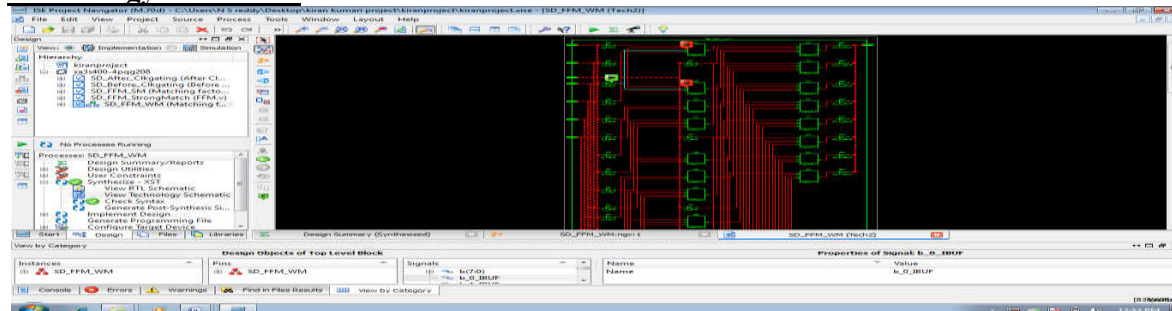


## 4. Weak matching

### Rtl schematic:

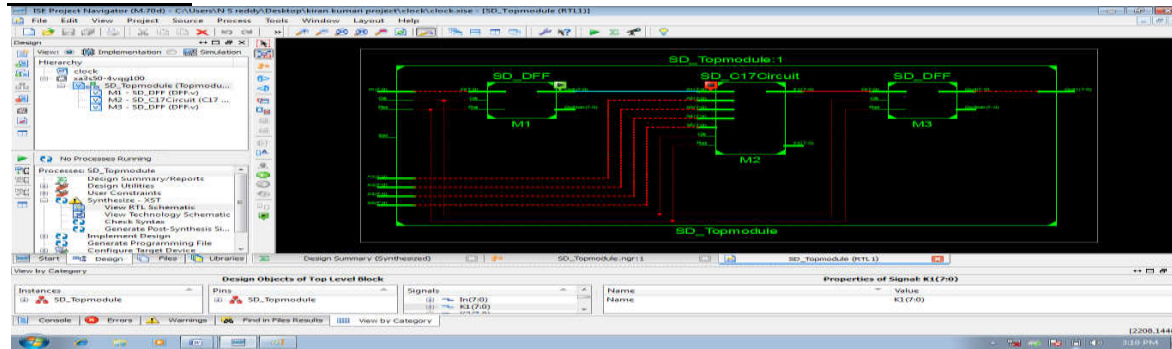


### Technology schematic:

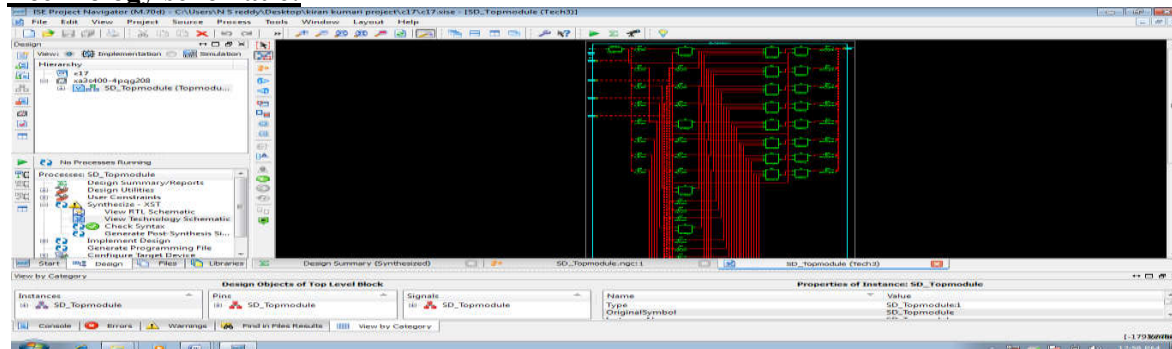


## 5 c17 circuit:

### Rtl schematic:



### Technology schematic:



## CONCLUSION

Gate-level clock gating synthesis is not yet in main stream use, but is a promising methodology due to its convenience offered to designers. New solutions for two key problems of the synthesis, merge and simplification, have been proposed. The iteration of minimum weight perfect matching formulation yields balanced grouping of flip-flops without too much decrease in average gating probability; this is in an effort to overcome the limitation of greedy approach to merge. Factored form matching has been proposed to utilize existing combinational logic as much as possible, this is an extension of a prior method using Boolean division.

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